

Distribution	Notation	$supp(X)$	$\Theta$	p.f.	$E(X)$	$Var(X)$	m.g.f.
Bernoulli	$Ber(\theta)$	$\{0, 1\}$	$[0, 1]$	$\theta^x(1-\theta)^{1-x}$	$\theta$	$\theta(1-\theta)$	$(1-p) + pe^t$
Binomial	$Bin(n, p)$	$\{0, 1, \dots, n\}$	$\mathbb{N} \times [0, 1]$	$\binom{n}{x}\theta^x(1-\theta)^{n-x}$	$n\theta$	$n\theta(1-\theta)$	$[(1-p) + pe^t]^n$
Discrete Uniform	$DU(n)$	$\{1, 2, \dots, n\}$	$\mathbb{N}$	$\frac{1}{n}$	$\frac{n+1}{2}$	$\frac{(n+1)(n-1)}{12}$	$\frac{1}{n} \sum_{i=1}^n e^{it}$
Geometric	$Geom(\theta)$	$1, 2, \dots$	$[0, 1]$	$\theta(1-\theta)^{x-1}$	$\frac{1}{\theta}$	$\frac{1-\theta}{\theta^2}$	$\frac{\theta e^t}{1-(1-\theta)e^t}$ , $t < -\log(1-\theta)$ .
Hypergeometric	$HGeom(n, m, k)$	$0, 1, \dots$	$[0, \infty)^3$	$\theta(1-\theta)^x$	$\frac{1-\theta}{\theta}$	$\frac{1-\theta}{\theta^2}$	$\frac{\theta}{1-(1-\theta)e^t}$
		$\{0, 1, \dots, k\}$		$\frac{\binom{m}{x}\binom{n-m}{k-x}}{\binom{n}{k}}$	$\frac{km}{n}$	$\frac{km}{n} \frac{(n-m)(n-k)}{n(n-1)}$	<b>too ugly</b>
Negative Binomial	$NegBin(r, \theta)$	$m - (n - k) \leq x \leq m$ , $0, 1, \dots$	$(0, \infty) \times [0, 1]$	$\binom{r+x-1}{x}\theta^r(1-\theta)^x$	$\frac{r(1-\theta)}{\theta}$	$\frac{r(1-\theta)}{\theta}$	$\left(\frac{\theta}{1-(1-\theta)e^t}\right)^r$ , $t < -\log(1-\theta)$ .
Poisson	$Poisson(\theta)$	$0, 1, \dots$	$[0, \infty)$	$\frac{e^{-\theta}\theta^x}{x!}$	$\theta$	$\theta$	$e^{\theta(e^t-1)}$ .

Table 1: Discrete distributions

Distribution	Notation	$supp(X)$	$\Theta$	p.d.f.	$E(X)$	$Var(X)$	m.g.f.
Normal	$N(\mu, \sigma^2)$	$\mathbb{R}$	$\mathbb{R} \times (0, \infty)$	$\frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{1}{2}\left(\frac{x-\mu}{\sigma}\right)^2}$	$\mu$	$\sigma^2$	$e^{\mu t + \sigma^2 t^2 / 2}$
Uniform	$U(a, b)$	$[a, b]$	$\mathbb{R}^2$ $a < b$	$\frac{1}{b-a}$	$\frac{b+a}{2}$	$\frac{(b-a)^2}{12}$	$\frac{e^{bt} - e^{at}}{(b-a)^t}$
Beta	$Beta(a, b)$	$[0, 1]$	$(0, \infty)^2$	$\frac{\Gamma(a+b)}{\Gamma(a)\Gamma(b)} x^{a-1} (1-x)^{b-1}$	$\frac{a}{a+b}$	$\frac{ab}{(a+b)^2(a+b+1)}$	$1 + \sum_{k=1}^{\infty} \left( \prod_{r=0}^{k-1} \frac{a+r}{a+b+r} \right) \frac{t^k}{k!}$
Exponential	$exp(\theta)$	$[0, \infty)$	$(0, \infty)$	$\theta e^{-\theta x}$	$\frac{1}{\theta}$	$\frac{1}{\theta^2}$	$\frac{\theta}{\theta-t},$ $t < \theta$ .
Gamma	$Gamma(a, \theta)$	$(0, \infty)$	$(0, \infty)^2$	$\frac{\theta^a}{\Gamma(a)} x^{a-1} e^{-\theta x}$	$\frac{a}{\theta}$	$\frac{a}{\theta^2}$	$\left(\frac{\theta}{\theta-t}\right)^a,$ $t < \theta$ .
Inverse Gamma	$IG(a, b)$	$(0, \infty)$	$(0, \infty)^2$	$\frac{1}{\Gamma(a)\theta^a} x^{a-1} e^{-\frac{x}{\theta}}$	$a\theta$	$a\theta^2$	$\left(\frac{1}{1-\theta t}\right)^a,$ $t < \frac{1}{\theta}$ .
Pareto	$Pareto(a, b)$	$(a, \infty)$	$(0, \infty)^2$	$\frac{b^a}{\Gamma(a)} \left(\frac{1}{x}\right)^{a+1} e^{-\frac{b}{x}}$	$\frac{b}{a-1}$ $a > 1$	$\frac{b^2}{(a-1)^2(a-2)}$ $a > 2$ .	$\left(\frac{1}{1-bt}\right)^a,$ $t < \frac{1}{b}$ .
t-Student	$t_\nu$	$\mathbb{R}$	$1, 2, \dots$	$\frac{1}{\Gamma(a)b^a} x^{a-1} e^{-\frac{x}{b}}$	$ab$	$ab^2$	does not exist.
Chi squared	$\chi_\nu^2$	$[0, \infty)$	$1, 2, \dots$	$\frac{\Gamma(\frac{\nu+1}{2})}{\Gamma(\frac{\nu}{2})} \frac{1}{\sqrt{\nu\pi}} \left(1 + \frac{x^2}{\nu}\right)^{-\frac{(\nu+1)}{2}}$	$\frac{ab}{b-1}$ $0$ $\nu > 1$	$\frac{a^b}{(b-1)^2(b-2)}$ $\frac{\nu}{\nu-2}$ $\nu > 2$ .	does not exist.
Cauchy	$Cauchy(\theta, \sigma)$	$\mathbb{R}$	$\mathbb{R} \times (0, \infty)$	$\frac{1}{\pi\sigma} \frac{1}{1 + \left(\frac{x-\theta}{\sigma}\right)^2}$	does not exist	does not exist	$\left(\frac{1}{1-2t}\right)^{p/2},$ $t < 1/2$ .

Table 2: Continuous distributions